

# VLE and LLE Data Set for the System Cyclohexane + Cyclohexene + Water + Cyclohexanol + Formic Acid + Formic Acid Cyclohexyl Ester

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The six-component system cyclohexene + water + cyclohexanol + cyclohexane + formic acid + formic acid cyclohexyl ester is currently being studied with the aim of carrying out the reaction of cyclohexene and water to cyclohexanol in a reactive distillation (RD) column. Because the direct reaction path of cyclohexene hydration is strongly limited by slow reaction rates with the known catalysts, an intermediate ester-formation step with formic acid was included in the studies. The challenge that this six-component system poses for a reactive separator such as an RD column lies in the liquid–liquid phase splitting behavior. This adds a third effect besides reaction and distillation. Cyclohexane is included in these studies to represent any inert C<sub>6</sub> components present under industrial conditions. To be able to design an RD column, measurements were conducted of the liquid–liquid and vapor–liquid equilibria, and appropriate NRTL parameters matching both vapor–liquid and liquid–liquid phase splitting behavior were identified.

## Introduction

Cyclohexanol is an important chemical intermediate in nylon production. As was discussed in a previous paper,<sup>1</sup> its current production route has many drawbacks such as low selectivity even at low conversions, high energy consumption, and explosion risks. As was argued there, integrating reaction and separation and using the hydration reaction of cyclohexene to form cyclohexanol in a reactive distillation process could potentially solve all of these problems. This step would presumably lead to a significant reduction in both investment and operational costs.

Unluckily, however, the reaction needs a very strong acidic catalyst to reach sufficient reaction rates for a technical process. Preliminary experiments with different catalysts have shown that the catalysts are either very fine particles of less than 1 μm diameter, which are very hard to immobilize in a column without deactivation, or they are in the millimeter range but do not show sufficient activity for economic column operation. So far no catalyst that is both active enough and easy to integrate into a column is available.

This lack of a technically feasible catalyst was the reason to carry out the reaction with the help of an intermediate step. This step is the reaction of cyclohexene with formic acid to produce formic acid cyclohexyl ester (FCE), which is then split in a reverse esterification reaction under the addition of water to cyclohexanol and formic acid. The net reaction is still the hydration of cyclohexene to cyclohexanol; formic acid can be seen as a reactive entrainer that takes part in the reaction but is recycled. The reaction rates in this two-step reaction scheme are significantly higher,

allowing the use of a conventional acidic ion-exchange resin as a catalyst for both steps.

For the design of a suitable coupled-column system for cyclohexanol synthesis and purification, a consistent description of the vapor– and liquid–liquid equilibria is of high importance. In our previous paper,<sup>1</sup> VLE and LLE data for the original four-component mixture was presented as well as NRTL parameters that describe both phenomena well. This four-component system is now expanded to six components, incorporating FCE and formic acid as additional components.

An interesting aspect of this system is the paucity of available data for FCE in the literature. This forced us to measure many parameters that are usually available. Specifically, it was not possible to find an Antoine parameter set or any solubility or VLE data for FCE. For formic acid, however, reliable VLE data was available for the binary mixture with water.<sup>2–4</sup> Data on the other binary pairs could not be found, however.

For this reason, VLE measurements were performed for the binary pairs cyclohexene + FCE, cyclohexanol + FCE, and cyclohexane + FCE. Because of the good literature data for formic acid + water, no further VLE measurements of this binary pair were made. Because water has a mixing gap with FCE and formic acid has mixing gaps with cyclohexene and cyclohexane, the following ternary LLE measurements were performed: cyclohexanol + water + FCE, cyclohexene + FCE + formic acid, water + FCE + formic acid, cyclohexanol + water + formic acid, and cyclohexane + FCE + formic acid.

The results of these measurements and a suggested set of NRTL<sup>7</sup> parameters to describe the six-component system are being presented here.

## Experimental Section

**Materials.** To measure both LLE and VLE data, synthesis-quality (>99%) cyclohexene, cyclohexanol, cyclohex-

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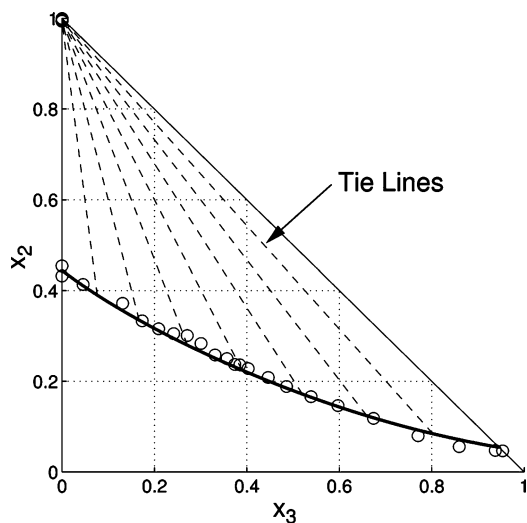
**Table 9. Measured and Calculated Vapor Pressures of FCE and Their Differences at Several Temperatures**

FCE			
<i>T</i> /K	<i>P</i> /mbar	<i>P</i> <sub>calc</sub> /mbar	Δ <i>P</i> /mbar
307.35	6.0	6.1	-0.1
316.55	10.0	10.5	-0.5
328.65	20.0	20.2	-0.2
342.50	40.0	40.0	0.0
358.05	80.0	79.4	0.6
375.65	159.0	158.6	0.4
395.55	318.0	316.9	1.1
418.50	638.0	638.0	0.0
434.95	998.0	997.8	0.2

**Table 10. Antoine Coefficients, Valid Temperature Range Δ*T*, and Standard Deviations between Measurements and Calculations for the Six Components<sup>a</sup>**

substance	<i>A</i>	<i>B</i>	<i>C</i>	Δ <i>T</i> /K	<i>σ</i> /mbar
cyclohexene	3.98075	1206.02	-52.7753	310-360	0.6374
cyclohexanol	4.06566	1258.75	-123.673	320-435	0.3293
water	5.00749	1605.78	-52.2025	300-375	1.0270
cyclohexane	3.96959	1191.56	-53.2741	305-355	0.9905
FCE	4.09578	1489.03	-71.4825	305-435	0.3437
formic acid	4.57631	1608.22	-21.8974	265-385	1.6700

<sup>a</sup> Antoine coefficients for formic acid were fitted to literature data.<sup>5,6</sup> Parameters for cyclohexene, cyclohexanol, water, and cyclohexane were taken from our previous publication.<sup>1</sup> The Antoine equation used was  $\log_{10}(P) = A - B/(T + C)$  for *P* in bars and *T* in K.

**Figure 1.** Comparison of the complete set of measurement data (circles) with the computed values (lines) using the NRTL parameter set of Table 11 for cyclohexanol (1) + water (2) + FCE (3) at ambient temperature (295 K) and pressure.

The equilibrium constant was computed via

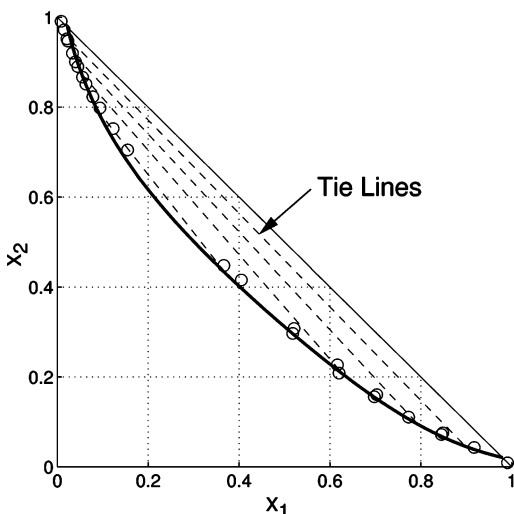
$$K_{\text{eq}} = k e^{-\Delta G_{\text{R}}/RT} = \frac{P_{\text{dimer}}}{P_{\text{monomer}}^2} \quad (1)$$

In this equation,  $K_{\text{eq}}$  is the equilibrium constant,  $k$  is a constant factor,  $\Delta G_{\text{R}}$  is the Gibbs enthalpy of reaction,  $R$  is the universal gas constant,  $T$  is the temperature in Kelvin, and the  $P$ s are the partial pressures in bar of the monomer and dimer, respectively. The parameters needed for this computation were fitted using data from the literature.<sup>8</sup> The value obtained for  $k$  was  $2.4726 \times 10^{-9}$  /bar; the value for  $\Delta G_{\text{R}}$  was  $-6.3766 \times 10^4$  J/mol. The saturation pressure computed via the Antoine equation is for the sum of the vapor pressures of the dimer and monomer.

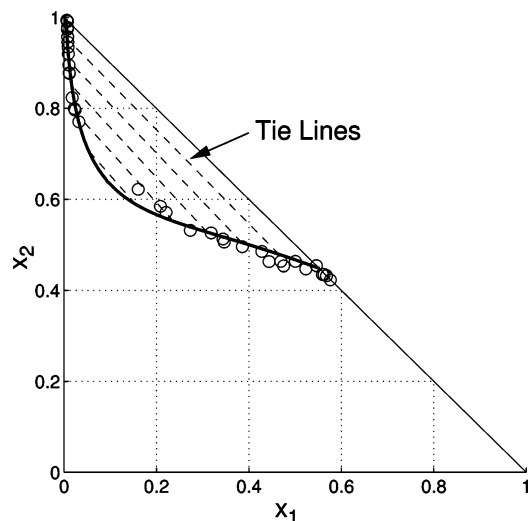
**Table 11. NRTL Parameters with Associated Standard Deviations between Different Measurement Types and Calculations for the Six Given Components<sup>a</sup>**

binary pair	$g_{12}$ /J/mol	$g_{21}$ /J/mol	$\alpha_{12}$	$\sigma_y$	$\sigma_P$ /mbar	$\sigma_{x,\text{LLE}}$	binary pair	$g_{12}$ /J/mol	$g_{21}$ /J/mol	$\alpha_{12}$	$\sigma_y$	$\sigma_P$ /mbar	$\sigma_{x,\text{LLE}}$
cyclohexene (1) + cyclohexanol (2)	3568.41	-0.962835	0.802522	0.0279	41.5	0.00497	cyclohexanol (1) + formic acid (2)	-1778.81	3290.04	0.689468	0.0154	56.6	0.00893 (4)
cyclohexene (1) + water (2)	14 175.4	21 695.0	0.267206	0.00386	9.20	0.0162 (2)	water (1) + cyclohexane (2)	25 048.5	17 650.0	0.258799	0.0154	56.6	0.00681
cyclohexene (1) + cyclohexane (2)	42.4813	60 957.2	0.831053	0.0120	29.7	0.0162 (2)	FCE (2)	15 899.1	5877.86	0.286963	0.0154	56.6	0.00458 (1)
cyclohexene (1) + FCE (2)	-2390.29	3308.21	0.215759	0.0120	29.7	0.0162 (2)	water (1) + formic acid (2)	3507.57	-4043.93	0.139498	0.0154	56.6	0.0120 (5)
cyclohexene (1) + formic acid (2)	7828.68	7619.60	0.342528	0.0151	131.7	0.0162 (2)	cyclohexane (1) + FCE (2)	3627.17	-2134.86	0.315477	0.0154	56.6	0.0162 (3)
cyclohexanol (1) + water (2)	1336.76	10 959.4	0.359706	0.0230	91.7	0.0162 (2)	cyclohexane (1) + formic acid (2)	10 153.6	9943.91	0.287689	0.0154	56.6	0.0120 (5)
cyclohexanol (1) + cyclohexane (2)	19.9341	4071.64	0.993301	0.0230	91.7	0.0162 (2)	FCE (1) + formic acid (2)	-415.705	3158.48	0.765244	0.0154	56.6	0.0162 (3)
cyclohexanol (1) + FCE (2)	1540.33	337.622	0.313377	0.0132	8.28	0.0162 (2)							

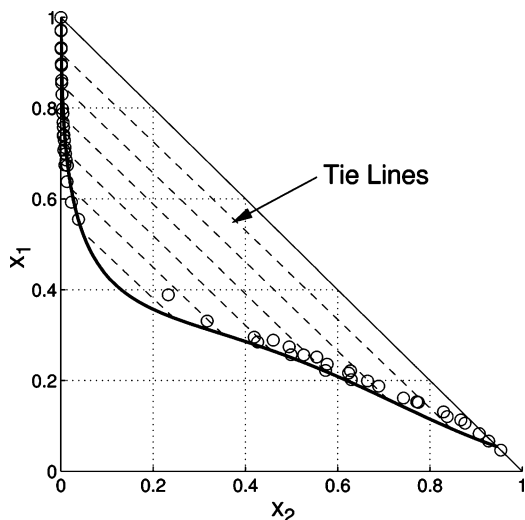
<sup>a</sup> The numbers in parentheses behind the  $\sigma_{x,\text{LLE}}$  figures denote the Table or Figure that these values are computed for because these are actually from ternary mixtures.



**Figure 2.** Comparison of the complete set of measurement data (circles) with the computed values (lines) using the NRTL parameter set of Table 11 for cyclohexene (1) + FCE (2) + formic acid (3) at ambient temperature (295 K) and pressure.



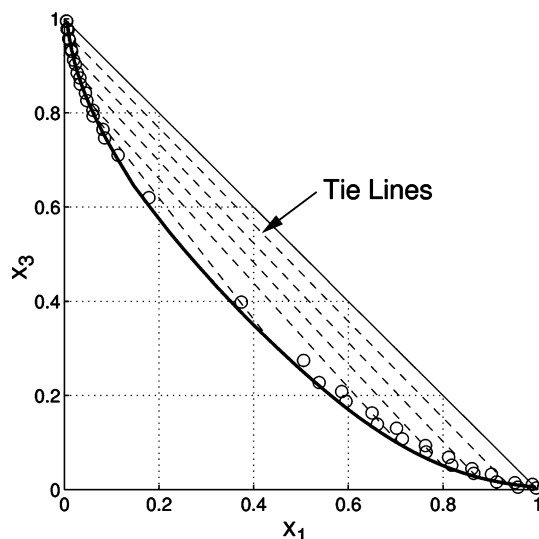
**Figure 4.** Comparison of the complete set of measurement data (circles) with the computed values (lines) using the NRTL parameter set of Table 11 for cyclohexanol (1) + water (2) + formic acid (3) at a temperature of 278 K and ambient pressure.



**Figure 3.** Comparison of the complete set of measurement data (circles) with the computed values (lines) using the NRTL parameter set of Table 11 for water (1) + FCE (2) + formic acid (3) at ambient temperature (295 K) and pressure.

Because of the large number of data and parameters that were to be fitted to one another, a subset approach was introduced into the optimization. This means that for any given binary, ternary, or quaternary subsystem for which the parameters were to be fitted the appropriate data subset was generated including all data that can have an influence on the appropriate parameter set. This allowed us to reduce the computational effort in finding the parameter sets significantly and to make the task parallel to some extent. The computational effort was still considerable, and there might exist a parameter set that describes the data even better than the one presented here. As a final fine-tuning step of the 45 parameters, a maximum likelihood approach was applied to the overall data set and all parameters simultaneously that led to a slight quality increase of the fit.

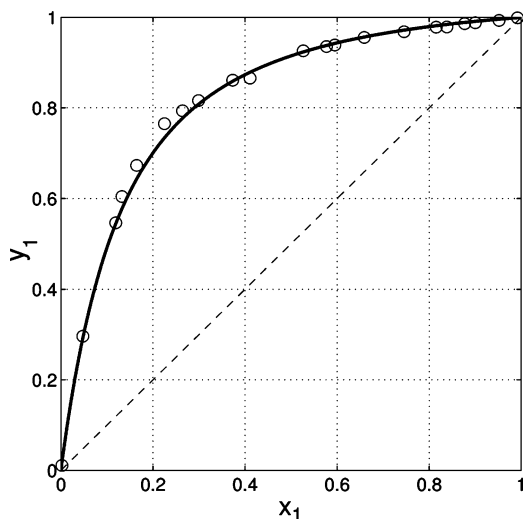
Because the data of the four-component system were included in the optimization, a change in the resulting parameter set is visible. This mainly reflects the influence that the new data has on the overall optimization. For this reason, the whole parameter set consisting of 45 parameters is reported here as Table 11.



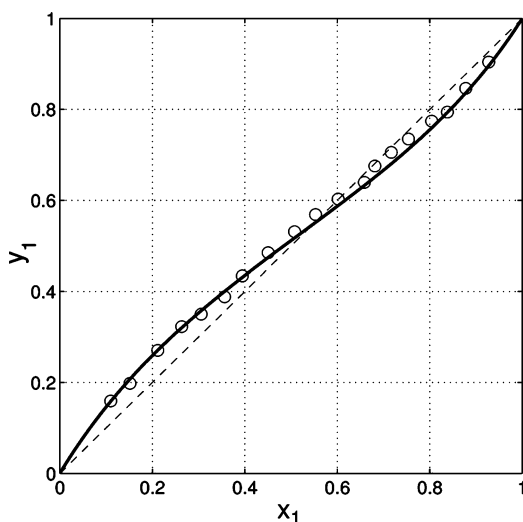
**Figure 5.** Comparison of the complete set of measurement data (circles) with the computed values (lines) using the NRTL parameter set of Table 11 for cyclohexene (1) + FCE (2) + formic acid (3) at ambient temperature (295 K) and pressure.

**Simulated Results vs Experimental Results.** The optimized parameter set of Table 11 was used to compute the binodal curves for the ternary systems that had been measured. The comparison of the measurement data and the computations using this parameter set can be found as Figures 1 to 5. The changes in the binodal curves of the cyclohexene + cyclohexanol + water and cyclohexanol + water + cyclohexane systems were so small that they were practically indistinguishable from the curves plotted in our previous paper,<sup>1</sup> so they are not shown again here.

Computations of the McCabe–Thiele diagrams were also performed for the measured systems. These plots compare the computations with the measurements and can be found as Figures 6 to 8. The comparison for water + formic acid was not shown because the literature data used was measured at quite different pressures and would thus give multiple curves and thus multiple figures. The fit of the computations to the literature measurements was of similar quality to that of the other binary pairs, however. Overall, the quality of the fits to the measurement data can be seen to be very good, especially when considering



**Figure 6.**  $x$ - $y$  diagram of the system cyclohexene (1) + FCE (2). The circles show the complete set of measured values at ambient pressure and the curve the fitted NRTL interpolation using the parameter set of Table 11 at average pressure (1012 mbar).

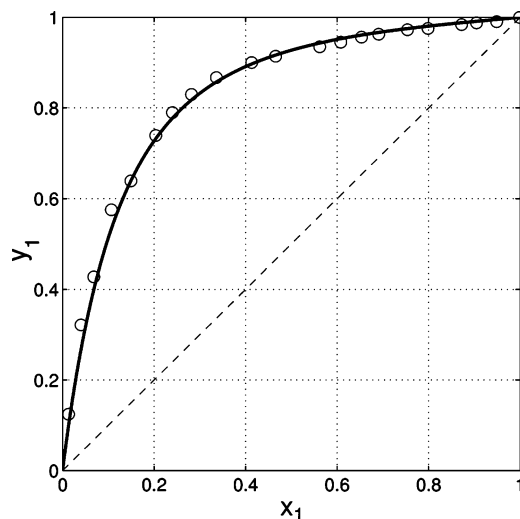


**Figure 7.**  $x$ - $y$  diagram of the system cyclohexanol (1) + FCE (2). The circles show the complete set of measured values at ambient pressure and the curve the fitted NRTL interpolation using the parameter set of Table 11 at average pressure (1014 mbar).

that the same parameter set is being used to describe the VLE and LLE behavior.

## Conclusions

The binary vapor-liquid equilibria for cyclohexene + FCE, cyclohexanol + FCE, and cyclohexane + FCE were measured at ambient pressure. Also, liquid-liquid equilibria were measured for the ternary systems cyclohexanol + water + FCE, cyclohexene + FCE + formic acid, water + FCE + formic acid, cyclohexanol + water + formic acid, and cyclohexane + FCE + formic acid. The first of these five ternary systems shows type II phase behavior; the other four show type I phase behavior. The  $P$ ,  $T$  relationship of FCE was measured. Parameters for Antoine's equation were computed for FCE and formic acid, for which the measurement data was taken from the literature. A



**Figure 8.**  $x$ - $y$  diagram of the system cyclohexane (1) + FCE (2). The circles show the complete set of measured values at ambient pressure and the curve the fitted NRTL interpolation using the parameter set of Table 11 at average pressure (1005 mbar).

set of 45 NRTL parameters was computed that describe the overall phase behavior well.

The six-component system shows six heteroazeotropes, an additional low-boiling azeotrope between cyclohexanol + FCE, and a high-boiling azeotrope between formic acid + water. Cyclohexanol as the desired product has the same boiling point as FCE and has an azeotrope with it. For this reason, a reactive separator has to be designed very carefully to yield pure cyclohexanol as a product.

## Acknowledgment

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